

# On Parameters Settings in Multi-Robot Exploration Strategies

**Jan Faigl, Petr Vaněk**

Laboratory for Computational Robotics  
Agent Technology Center / Department of Computer Science  
Czech Technical University in Prague

August 18, 2014



# Outline

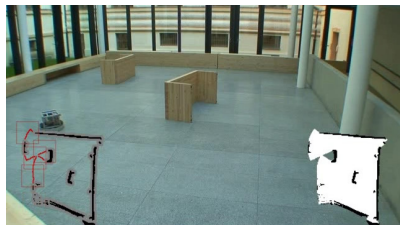
- Multi-Robot Exploration - problem formulation
- Overview of the goal assignment methods
- Local decision-making towards global optimization
  - Distance cost vs time to travel
  - Task-allocation with return to depot
  - Goal assignment with small number of goal candidates
- Influence of replanning period
- Evaluation methodology and results



# Multi-Robot Exploration of Unknown Environment

A problem to create a map of the given unknown environment

- **Frontier**-based approach  
*Yamauchi (1997)*
- Occupancy grid  
*Moravec and Elfes (1985)*
- Laser scanner sensor
- Next-best-view approach  
*Select the next robots' goals*



Performance metric:

**Time to create the map of the whole environment**

*search and rescue mission*



# Multi-Robot Exploration as Task-Allocation Problem

At the time  $t$  of the local decision-making we have:

- A current map of the environment  $\mathcal{M}$
- A set of  $m$  robots at positions  $\mathbf{R}(t) = \{r_1, r_2, \dots, r_m\}$
- A set of  $n$  goal candidates be  $\mathbf{G}(t) = \{g_1, \dots, g_n\}$

*e.g., frontiers*

We need to assign a goal  $g \in \mathbf{G}(t)$  for each robot  $r \in \mathbf{R}(t)$  that will minimize the required time to explore the environment.

The problem is formulated as the **task-allocation problem**

$$(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \text{assign}(\mathbf{R}(t), \mathbf{G}(t), \mathcal{M}),$$

*We call the determination of  $\mathbf{G}$  and assignment procedure the **exploration strategy**.*

We consider only the distance cost for the assignment



# Multi-Robot Exploration as Task-Allocation Problem

At the time  $t$  of the local decision-making we have:

- A current map of the environment  $\mathcal{M}$
- A set of  $m$  robots at positions  $\mathbf{R}(t) = \{r_1, r_2, \dots, r_m\}$
- A set of  $n$  goal candidates be  $\mathbf{G}(t) = \{g_1, \dots, g_n\}$

*e.g., frontiers*

We need to assign a goal  $g \in \mathbf{G}(t)$  for each robot  $r \in \mathbf{R}(t)$  that will minimize the required time to explore the environment.

The problem is formulated as the **task-allocation problem**

$$(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \text{assign}(\mathbf{R}(t), \mathbf{G}(t), \mathcal{M}),$$

*We call the determination of  $\mathbf{G}$  and assignment procedure the **exploration strategy**.*

**We consider only the distance cost for the assignment**

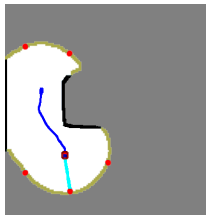


## Distance Cost Variants

### Simple robot–goal distance

- A length of the robot-goal candidate path
- Greedy goal selection

*Select the closest goal candidate*



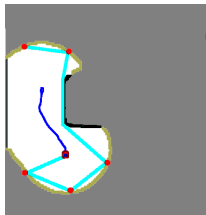
### TSP distance cost



Kulich M., Faigl J., Přeučil L.,  
*On Distance Utility in the Exploration Task*,  
 ICRA, 2011, 4455–4460.

- Consider visitations of all goal candidates  
*Solve the associated traveling salesman problem (TSP)*
- A length of the tour visiting all goals
- **Goal representatives**

*TSP distance cost improves performance about 10-30%*

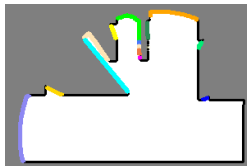
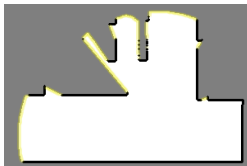


# Goal Candidates Determination

## RFE – Representative of Free Edges

*Kulich & Faigl & Preucil, ICRA (2011)*

- Organize frontier cells into free edges  $F_i$
- Select representatives of  $F_i$  from which  $F_i$  would be covered
  - Means of  $n_r$  clusters found by K-means algorithm



*RFE is necessary for the TSP distance cost, but it also improves performance of other task-allocation methods.*



Faigl J., Kulich M.

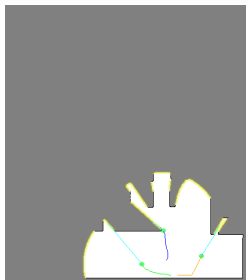
*On determination of goal candidates in frontier-based multi-robot exploration,*

ECMR, 2013, 210–215.



## Multi-Robot Exploration Procedure

1. Initialize occupancy grid  $\mathcal{O}_{cc}$  and robot plans  $\mathcal{P} = (P_1, \dots, P_m)$
2. Repeat
  - 2.1 Navigate robots regarding  $\mathcal{P}$
  - 2.2 Update  $\mathcal{O}_{cc}$  with new sensor measurements (with range  $\rho$ )
 Until **replanning condition**.



3. Update the navigation map  $\mathcal{M}$  from the current  $\mathcal{O}_{cc}$ .
4. Detect all frontiers  $\mathcal{F}$  in the current map  $\mathcal{M}$ .
5. **Determine goal candidates  $\mathbf{G}(t)$**  from the frontiers  $\mathcal{F}$ .
6. If  $|\mathbf{G}(t)| > 0$  **assign goals to the robot**
  - $(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \text{assign}(\mathbf{R}(t), \mathbf{G}(t), \mathcal{M})$
  - Plan paths  $\mathcal{P} = \text{plan}(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle, \mathcal{M})$
  - Go to Step 2.
7. Stop all robots





# Goal Assignment Methods

## 1. **GA** – Greedy assignment

*Yamauchi B, Robotics and Autonomous Systems 29, 1999*

- Randomized greedy selection of the closest goal candidate

## 2. **IA** – Iterative assignment

*Werger B, Mataric M, Distributed Autonomous Robotic Systems 4, 2001*

- Centralized variant of the broadcast of local eligibility (BLE)
- Ordering of all robot-goal pairs  $\langle r, g \rangle$

## 3. **HA** – Hungarian assignment

- Optimal solution of the task-allocation problem

*Stachniss C, C implementation of the Hungarian method, 2004*

## 4. **MA** – Multiple Traveling Salesman Problem assignment

- Based on TSP distance cost
- $\langle \text{cluster-first, route-second} \rangle$  heuristic based on K-means



Faigl J., Kulich M., Přeučil L.

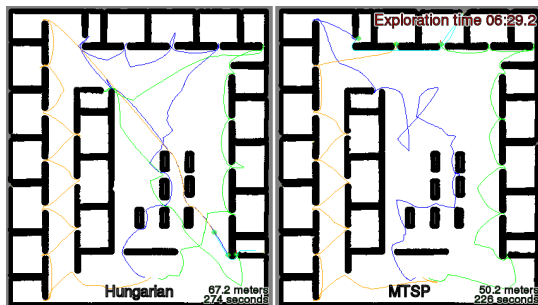
*Goal Assignment using Distance Cost in Multi-Robot Exploration,*

*IROS, 2012, 3741–3746.*



## Example of Multi-Robot Exploration

Objective function: time to complete the exploration



*Faigl, Kulich, Přeučil, IROS'12*

- Local planner based on Smooth Nearness-Diagram (SND)

*Durham, Bullo, IROS'08*

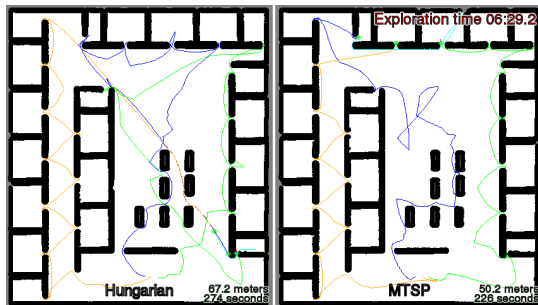
- Notice, robots are slow in doors

Goals assignment is based on robot-goal distances while we are minimizing the required time to complete exploration.



## Example of Multi-Robot Exploration

Objective function: time to complete the exploration



*Faigl, Kulich, Přeučil, IROS'12*

- Local planner based on Smooth Nearness-Diagram (SND)

*Durham, Bullo, IROS'08*

- Notice, robots are slow in doors

Goals assignment is based on robot-goal distances while we are minimizing the required time to complete exploration.



# Local Decision-Making and Global Optimality

- We aim to minimize a global objective function using local decision-making

*It's because we collect new information during the mission*

- The objective function is optimized indirectly based on the **next-best-view** approach
- A longer planning horizon in the TSP distance cost improves the exploration performance

What are other options to improve the performance by “better” local decisions?



# Local Decision-Making and Global Optimality

- We aim to minimize a global objective function using local decision-making

*It's because we collect new information during the mission*

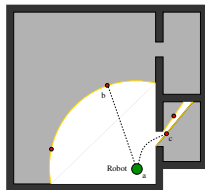
- The objective function is optimized indirectly based on the **next-best-view** approach
- A longer planning horizon in the TSP distance cost improves the exploration performance

What are other options to improve the performance by “better” local decisions?



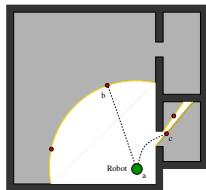
# Distance Cost vs Time to Travel in Goal Assignment

- Does time to travel provide better exploration performance?
- Not necessarily, it depends on the motion model
  - Path to *b* is longer, but faster
  - Path to *c* is shorter, but slower
- Distance cost with assumption of some average speed of the robots
- Distance cost for task-allocation and time as the objective function



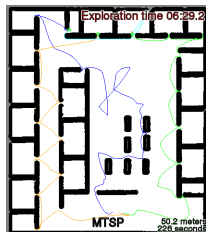
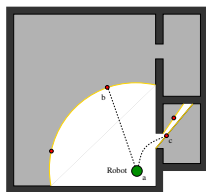
# Distance Cost vs Time to Travel in Goal Assignment

- Does time to travel provide better exploration performance?
- **Not necessarily, it depends on the motion model**
  - Path to *b* is longer, but faster
  - Path to *c* is shorter, but slower
- Distance cost with assumption of some average speed of the robots
- Distance cost for task-allocation and time as the objective function



# Distance Cost vs Time to Travel in Goal Assignment

- Does time to travel provide better exploration performance?
- Not necessarily, it depends on the motion model
  - Path to *b* is longer, but faster
  - Path to *c* is shorter, but slower
- Distance cost with assumption of some average speed of the robots
- Distance cost for task-allocation and time as the objective function





## Exploration with the Return to Depot

- The robots collect a large dataset during the exploration  
*e.g., high resolution images*
- The dataset cannot be transmitted due to a limited communication bandwidth
- The robots are requested to return to the depot at the end of the mission

*Bautin et al., IROS'13*

- We propose modifications of the local decision-making:
  - **HAd** – the cost for the goal assignment is computed as
$$c(r, g) = d(r, g) + d(g, depot) + traveled\_distance(r).$$
  - **MAd** – the TSP distance cost include a return trip from the last goal of the route to the depot



## Exploration with the Return to Depot

- The robots collect a large dataset during the exploration  
*e.g., high resolution images*
- The dataset cannot be transmitted due to a limited communication bandwidth
- The robots are requested to return to the depot at the end of the mission

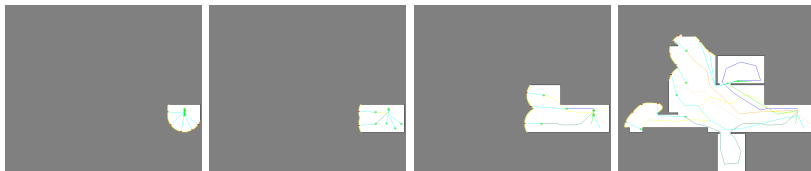
*Bautin et al., IROS'13*

- We propose modifications of the local decision-making:
  - **HAd** – the cost for the goal assignment is computed as
$$c(r, g) = d(r, g) + d(g, depot) + traveled\_distance(r).$$
  - **MAd** – the TSP distance cost include a return trip from the last goal of the route to the depot

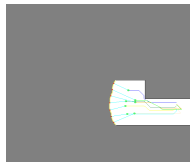


## Too Few Goals

- Robots without assigned goal move back to the depot
- RFE does not consider number of robots in the team
- The robots may move back to the depot too soon



- A modification of the RFE with the adaptive number of representatives (**ANR**) that increase number of goal candidates of the largest free edges



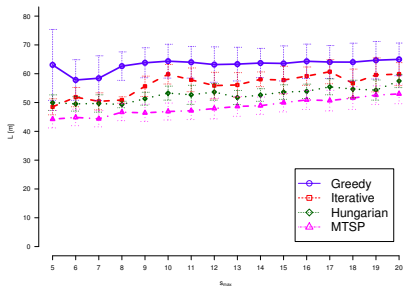
*Time reduction from 1744 to 1556 discrete time steps*



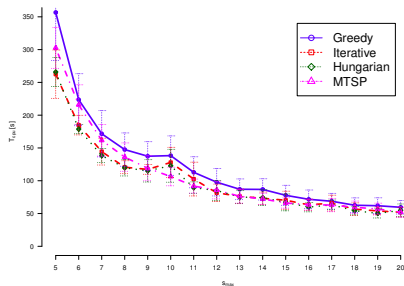
# Influence of the Replanning Period

$s_{max}$  – the replanning period in the number of motion primitives

(*move forward / turn*)



Average traveled distance  $L$



Required computational time  
3.2 GHz CPU

Performance of the exploration mission depends on the computational resources and also speed of the robots.



# Replanning Conditions

Two replanning conditions are studied:

- **GR** – Goal Replanning
  - Replanning when a robot reaches its goal
  - Computationally inexpensive
- **IR** – Immediate Replanning
  - Replanning whenever a goal is no longer frontier
  - Fastest replanning possible
  - Computationally very demanding



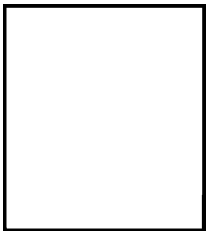
## Evaluation Methodology

- A discrete event based simulator allowing evaluation of the computationally demanding strategies without influence of the limited computational resources
- Perturbations of the initial robot positions (20 variants)
- 4 environments: *em* - empty, *autolab*, *jh* – structured, *pot-holes* – unstructured
- No. of robots  $m \in \{3, 5, 7\}$ , visibility range  $\rho \in \{3m, 5m, 7m\}$
- 6 assignment strategies: **GA**, **IA**, **HA**, **MA**, **HAd**, **MAd**
- 2 goal candidates determination methods: **RFE**, **ANR**
- 2 types of missions: open paths (**OP**) and return depot (**RD**)
- 2 variants of replanning: goal replanning (**GR**) and immediate replanning (**IR**)
- Statistical evaluation of 362 880 trials

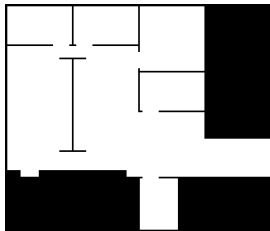
*20 trials per problem for stochastic strategies*



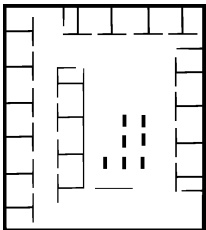
## Testing Environments



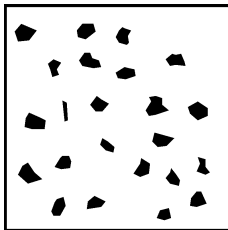
*em*



*autolab*



*jh*

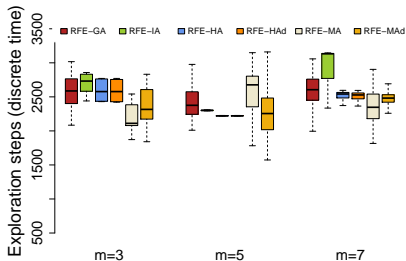


*potholes*

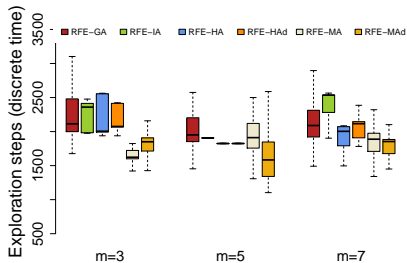


## Results – Return to Depot

- Selected results for *jh* environment, visibility range  $\rho=7$  m,
- Goal replanning (GR), and RFE goal candidates determination



return depot (RD) missions



open paths (OP) missions

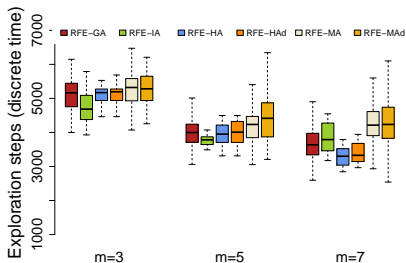
- HAd and MAd strategies do not provide expected benefits *in general*
- Modifications may occasionally improve the performance



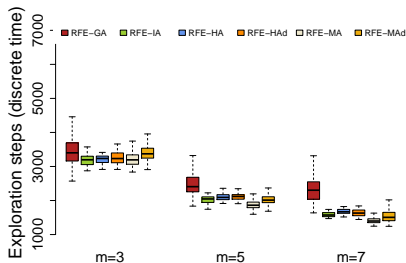


## Results – Replanning Period

- Selected results for *potholes* environment, visibility range  $\rho=3$  m,
- Open paths (OP), and RFE goal candidates determination



Goal replanning (**GR**)



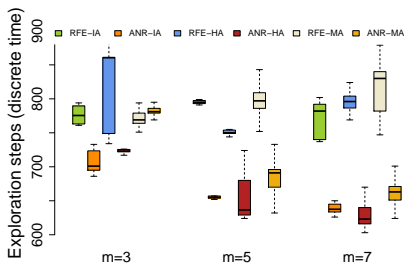
Immediate replanning (**IR**)

- Faster replanning significantly improves the performance
- A results of strategies comparison depends on replanning

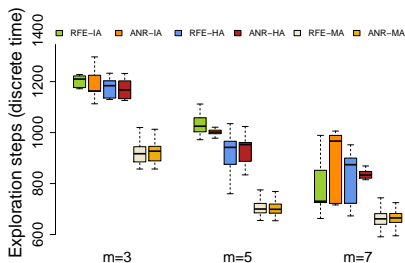


# Results – Adaptive Number of Representatives (ANR)

- Selected results for open paths (OP), and immediate replanning (IR)



*autolab,  $\rho = 7m$*



*jh,  $\rho = 5m$*

- Better in some cases, but mostly similar to RFE
- Provides a more stable the solution quality

*(smaller standard deviations)*



## Conclusion

- There are hidden issues of the local decision-making and global optimality (*distance vs time, return to depot*)  
*Approximations based on average expected performance provides better results than tailored decisions for local situations.*
- For large teams do not forget to generate sufficient number of goal candidates.
- Although simple centralized approaches have been evaluated, the evaluation and comparison of strategies can be still tricky.

Q1: Can we learn somehow the overall approximations that can be used for local decision-making?

Q2: Is there a way to compare and evaluate exploration strategies that will provide a generalizable results?

Q3: What evaluation methodology we should use?



## Conclusion

- There are hidden issues of the local decision-making and global optimality (*distance vs time, return to depot*)  
*Approximations based on average expected performance provides better results than tailored decisions for local situations.*
- For large teams do not forget to generate sufficient number of goal candidates.
- Although simple centralized approaches have been evaluated, the evaluation and comparison of strategies can be still tricky.

Q1: Can we learn somehow the overall approximations that can be used for local decision-making?

Q2: Is there a way to compare and evaluate exploration strategies that will provide a generalizable results?

Q3: What evaluation methodology we should use?



**Thank You!**

[faiglj@fel.cvut.cz](mailto:faiglj@fel.cvut.cz)

